

Lecture 6

Calorimetry & Thermochemistry



Suggested Reading

Thermochemistry

- Chemistry³, Chapter 14, Energy and Thermochemistry, pp.658-700.
- Elements of Physical Chemistry, 5th edition, Atkins & de Paula, Chapter 3, Thermodynamics: applications of the first law, pp. 63-82. Chapter 4. Thermodynamics: The Second Law, pp.83-104.
- Physical Chemistry, 8th Edition, Atkins & de Paula, The First Law, Chapter 2, pp.49-57 (Thermochemistry). Chapter 3, The Second Law, pp.76-116 (selected sections as indicated).
- Chemistry and Chemical Reactivity, Kotz, Treichel, Townsend, 7th edition, Chapter 5, pp.208-253, especially sections 5.7 and 5.8..

Refer to JF Chemistry 1101 laboratory manual thermochemistry experiment # 5
For further details.

HEAT CAPACITY

The heat required to raise an object's Temperature by 1 °C.



Which has the larger heat capacity?

Heat Capacity

Increasing temperature increases the internal energy of a system. The exact increase depends upon the heating conditions.

Heat cannot be detected or measured directly.
There is no 'heat meter'.

One way to determine the magnitude of a heat transfer is to measure the work needed to bring about the same change in the thermodynamic state of a system as was produced by heat transfer.

Another approach is to deduce the magnitude of a heat transfer from its effects: namely, a temperature change. When a substance is heated the temperature typically rises. For a specified energy q transferred by heating, the magnitude of the resulting temperature change ΔT depends on the heat capacity C of the substance.

We can therefore simply measure the heat absorbed or released by a system :

We determine the temperature change and use the appropriate value of the heat capacity of the system.

Units of C are $J K^{-1}$.

Heat capacity is an extensive property.

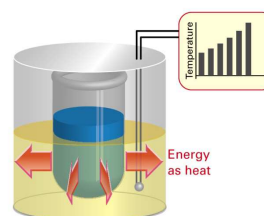
$$C = \frac{q}{\Delta T}$$

$$q = C\Delta T$$

Can also define specific heat capacity c according to $c = C/m$ where m = mass of substance with units

$J K^{-1}g^{-1}$ or the molar heat capacity C_m as $C_m = C/n$ with units: $J K^{-1}mol^{-1}$.

The heat capacity depends on whether a sample is maintained at constant volume ($C = C_V$) or constant pressure ($C = C_P$). The respective molar quantities are $C_{V,m}$ and $C_{P,m}$.



Loss of energy into the surroundings can be detected by noting whether the temperature changes as the process proceeds.

This is the principle of a calorimeter.

The bomb calorimeter

From the first law of thermodynamics we recall

$$\Delta U = q + w = q - P\Delta V$$

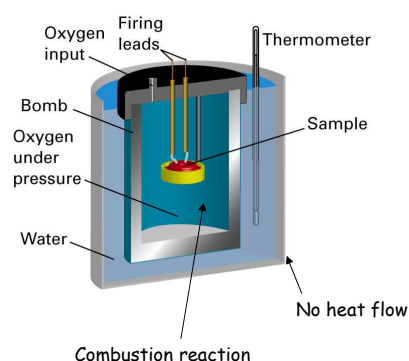
If the reaction is performed in a closed container called a bomb calorimeter then the volume remains constant and $\Delta V = 0$. Hence the first law reduces to

$$\Delta U = q_v$$

Hence to measure a change in internal energy we should use a fixed volume calorimeter and monitor the energy released ($q < 0$) or supplied ($q > 0$) as heat by measuring the corresponding change in temperature.

Chemistry³, Ch.14. pp.693-698

Kotz, section 5.6. pp.229-233.



$$C_v = \frac{q_v}{\Delta T} = \frac{\Delta U}{\Delta T}$$

$$C_v = \lim_{\Delta T \rightarrow 0} \frac{\Delta U}{\Delta T} = \frac{dU}{dT} = \left(\frac{\partial U}{\partial T} \right)_v$$

Calorimetry : some details.

Calorimetry defines the study of heat transfer during physical and chemical processes.

A calorimeter is a device for measuring energy transferred as heat. In an adiabatic bomb calorimeter the process which we wish to study (a chemical reaction) is initiated inside a constant volume container (the bomb). The latter is immersed inside a stirred water bath. The whole arrangement (container + water bath) defines the calorimeter. The calorimeter is also immersed in an outer water bath. The water in the calorimeter and in the outer water bath is monitored and adjusted to the same temperature. This arrangement ensures there is no net loss of heat from the calorimeter to the surroundings (the bath). Hence the calorimeter is adiabatic. The change in temperature ΔT of the calorimeter is proportional to the heat that the reaction releases or absorbs. Hence by measuring ΔT we can determine q_v and hence find ΔU .

We calibrate the calorimeter using a process of known energy output and determining the calorimeter constant C in the relation $q = C\Delta T$. The calorimeter constant may be measured electrically by passing a constant current I from a source of known potential difference V through a heater for a given period of time t and noting that $q = VI t$. Alternatively C may be determined by burning a known mass of substance (benzoic acid is often used) that has a known heat output. With C determined it is simple to interpret an observed temperature rise as a release of heat.

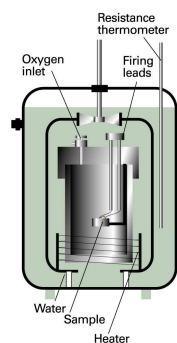
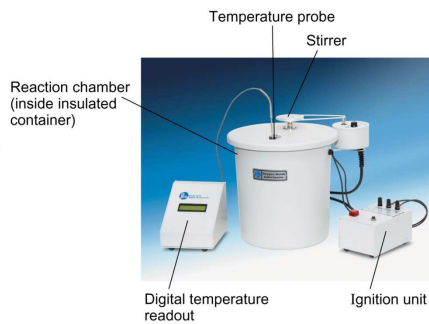
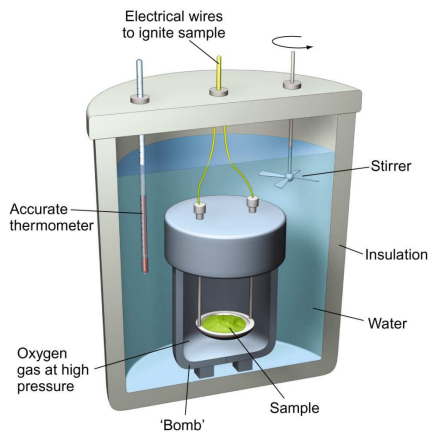
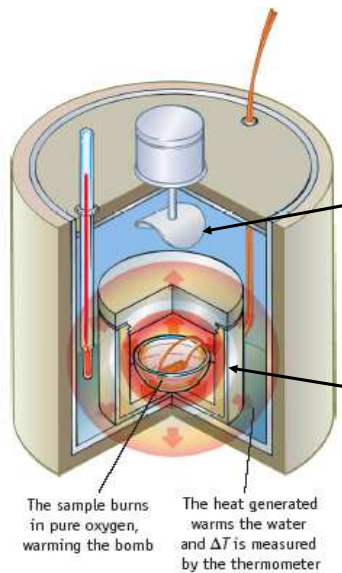


Fig. 2.9 A constant-volume bomb calorimeter. The 'bomb' is the central vessel, which is strong enough to withstand high pressures. The calorimeter (for which the heat capacity must be known) is the entire assembly shown here. To ensure adiabaticity, the calorimeter is immersed in a water bath with a temperature continuously readjusted to that of the calorimeter at each stage of the combustion.



A commercial bomb calorimeter.



Calorimetry

Some heat from reaction warms water
 $q_{\text{water}} = (\text{sp. ht.})(\text{water mass})(\Delta T)$

Some heat from reaction warms "bomb"
 $q_{\text{bomb}} = (\text{heat capacity, J/K})(\Delta T)$

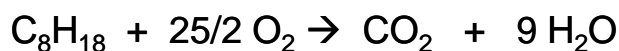
The sample burns in pure oxygen, warming the bomb

The heat generated warms the water and ΔT is measured by the thermometer

$$\text{Total heat evolved} = q_{\text{total}} = q_{\text{water}} + q_{\text{bomb}}$$

Measuring Heats of Reaction CALORIMETRY

Calculate energy of combustion (ΔU) of octane.



- Burn 1.00 g of octane
- Temp rises from 25.00 to 33.20 °C
- Calorimeter contains 1200. g water
- Heat capacity of bomb = 837 J/K

JF CH1101 Annual 2010 part d.

Measuring Heats of Reaction CALORIMETRY

Step 1 Calc. energy transferred from reaction to water.

$$q = (4.184 \text{ J/g}\cdot\text{K})(1200 \text{ g})(8.20 \text{ K}) = 41,170 \text{ J}$$

Step 2 Calc. energy transferred from reaction to bomb.

$$q = (\text{bomb heat capacity})(\Delta T) \\ = (837 \text{ J/K})(8.20 \text{ K}) = 6860 \text{ J}$$

Step 3 Total energy evolved

$$41,200 \text{ J} + 6860 \text{ J} = 48,060 \text{ J}$$

Energy of combustion (ΔU) of 1.00 g of octane

$$= - 48.1 \text{ kJ}$$

Enthalpy

Kotz, pp.225-229.

The change in internal energy is not equal to the energy transferred as heat when the system is free to change its volume. Under such circumstances some of the energy supplied as heat to the system is returned to the surroundings as expansion work.

We shall show that under constant pressure conditions, the energy supplied as heat is equal to the change in another thermodynamic property of the system, called the **enthalpy**.

From the first law of thermodynamics for a finite change at constant pressure

$$\Delta U = q + w = q_p - P\Delta V$$

Now $\Delta U = U_F - U_I$ $\Delta V = V_F - V_I$

Hence

$$U_F - U_I = q_p - P(V_F - V_I) = q_p - PV_F + PV_I$$

$$q_p = (U_F + PV_F) - (U_I + PV_I) = H_F - H_I = \Delta H$$

Here we have introduced the enthalpy function H as

$$H = U + PV$$

Hence the heat absorbed at constant pressure equals the increase in enthalpy of the system.

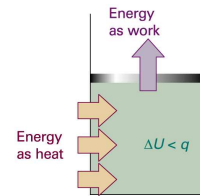


Fig. 2.12 When a system is subjected to constant pressure and is free to change its volume, some of the energy supplied as heat may escape back into the surroundings as work. In such a case, the change in internal energy is smaller than the energy supplied as heat.

$$q_p = \Delta H$$

For an exothermic reaction $\Delta U < 0$, $\Delta H < 0$, whereas for an endothermic reaction, $\Delta U > 0$ and $\Delta H > 0$.

Relationship between ΔU and ΔH .

The enthalpy is given by

$$H = U + PV$$

For a finite change at constant pressure

$$\Delta H = \Delta(U + PV) = \Delta U + \Delta(PV)$$

$$= \Delta U + P\Delta V + V\Delta P$$

$\Delta P = 0$
Constant P

$$= \Delta U + P\Delta V$$

Since $\Delta H = q_p$ $\Delta U = q_v$ we note that

$$q_p = q_v + P\Delta V$$

Hence the heat absorbed at constant pressure Exceeds that absorbed at constant volume by the Amount $P\Delta V$.

For condensed phases (liquids, solids) $\Delta V = V_{\text{products}} - V_{\text{reactants}}$ Will be very small and so $\Delta V \sim 0$. Hence

$$\Delta H \cong \Delta U$$

Condensed phases

Temperature variation of enthalpy.

The term ΔV is significant for gases.

Assume ideal gas behaviour. At constant T and P we have

$$PV = nRT$$

For reactants and products

$$PV_{R_x} = n_{R_x}RT$$

$$PV_{P_r} = n_{P_r}RT$$

Hence

$$P(V_{P_r} - V_{R_x}) = (n_{P_r} - n_{R_x})RT = \Delta nRT$$

where

$$\Delta n = n_{P_r} - n_{R_x}$$

Hence for gas phase species

$$\Delta H = \Delta U + \Delta nRT$$

$$C_p = \frac{q_p}{\Delta T} = \frac{\Delta H}{\Delta T}$$

$$C_v = \lim_{\Delta T \rightarrow 0} \frac{\Delta H}{\Delta T} = \frac{dH}{dT} = \left(\frac{\partial H}{\partial T} \right)_p$$

Thermochemistry

Thermochemistry is the branch of thermodynamics which studies heats of reaction: heat produced by or required for a chemical reaction.

In thermochemistry, chemical reactions are divided into two categories:

exothermic reaction

$q_{\text{rxn}} < 0$; heat is produced by the reacting system (i.e., the temperature of the system is higher right after the reaction than initially; heat must be transferred from the system to the surroundings in order to return the system to its initial temperature)

endothermic reaction

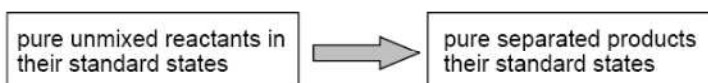
$q_{\text{rxn}} > 0$; heat is absorbed by the reacting system (i.e., the temperature of the system is lower right after the reaction than initially; heat must be transferred from the surroundings to the system in order to return the system to its initial temperature)

These reactions can also be described in terms of **enthalpy**, ΔH

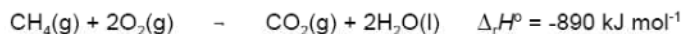
Enthalpies of Chemical Change

standard reaction enthalpy, $\Delta_r H^\circ$:

Change in enthalpy when reactants in standard states change to products in standard states



Example:



The change in enthalpy for the above **thermochemical equation** is for 1 mole of pure $\text{CH}_4(\text{g})$ reacting with 2 moles of pure $\text{O}_2(\text{g})$ at 1 bar to produce 1 mole of pure $\text{CO}_2(\text{g})$ and 2 moles of pure $\text{H}_2\text{O}(\text{l})$ at 1 bar

Changes in enthalpies of mixing and separation are insignificant compared to the standard reaction enthalpy, and may be neglected in this case

Hess's Law

Kotz, section 5.7, pp.233-239

Chemical reactions involve emission or adsorption of heat energy. We now discuss how these energy changes are calculated. Many chemical reactions are performed under conditions of constant pressure, so it is best to describe heat changes in terms of changes in enthalpy since $q_p = \Delta H$.

Enthalpy is a state function. As such ΔH going from some initial state to some final state is pathway independent so we can use any suitable pathway when calculating the enthalpy change associated with a chemical reaction.

Hence in going from a particular set of reactants to a particular set of products, the change in enthalpy is the same whether the reaction takes place in one step or in a series of steps.

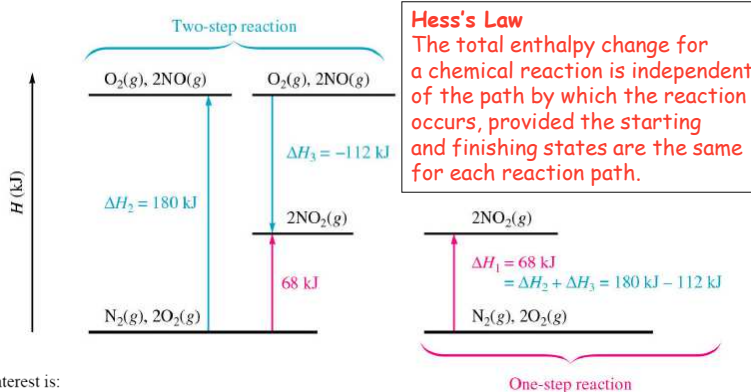
This principle is known as Hess's law.

To use Hess's Law to compute enthalpy changes for reactions we note:

1. If a reaction is reversed, the sign of ΔH is also reversed.
2. The magnitude of ΔH is directly proportional to the quantities of reactants and products in a reaction. If the coefficients in a balanced reaction are multiplied by an integer, the value of ΔH is multiplied by the same integer.

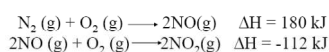
Formation of nitrogen dioxide.

Hess' Law: An Example

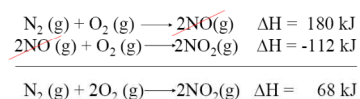


- Our reaction of interest is:
 $N_2(g) + 2O_2(g) \rightarrow 2NO_2(g) \quad \Delta H = 68 \text{ kJ}$

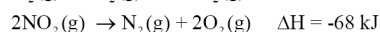
- This reaction can also be carried out in two steps:



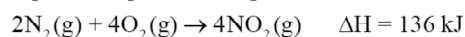
- If we take the previous two reactions and add them, we get the original reaction of interest:



- Note the important things about this example, the sum of ΔH for the two reaction steps is equal to the ΔH for the reaction of interest.
- Big point: We can combine reactions of known ΔH to determine the ΔH for the “combined” reaction.
- Once can always reverse the direction of a reaction when making a combined reaction. When you do this, the sign of ΔH changes.



- The magnitude of ΔH is directly proportional to the stoichiometric coefficients involved (it is proportional to the reaction as written).
- Therefore, if the coefficients of a reaction are multiplied by a constant, the value of ΔH is also multiplied by the same constant.

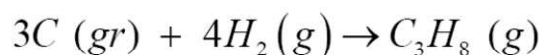


Enthalpy of formation of propane

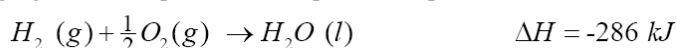
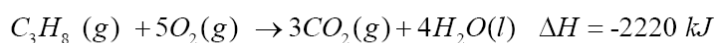
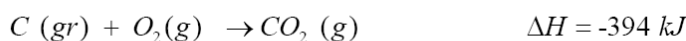
Using Hess' Law

- When trying to combine reactions to form a reaction of interest, one usually works **backwards** from the reaction of interest.
- Example:

What is ΔH for the following reaction?



You're given the following reactions:



Goal: Find how to add the three reactions to give the top reaction.

Approach: Find a thread through the equation for each starting and ending material. Eg: follow C(gr) to C₃H₈. Follow H₂ to C₃H₈. Use the target reaction as your way of finding the path that connects reactants and products.

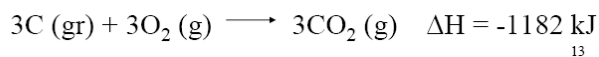
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- Step 1. Only reaction 1 has C (gr).
Therefore, we will multiply by 3 to get the correct amount of C (gr) with respect to our final equation.

Initial:



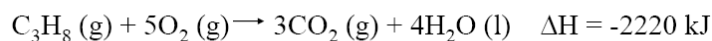
Final:



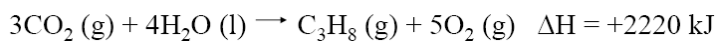
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- Step 2. To get C₃H₈ on the product side of the reaction, we need to reverse reaction 2.

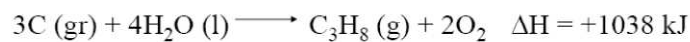
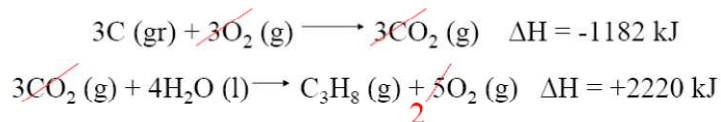
Initial:



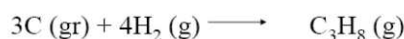
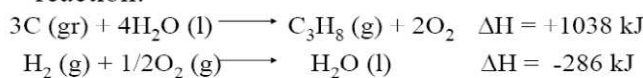
Final:



- Step 3: Add two “new” reactions together to see what is left:



- Step 4: Compare previous reaction to final reaction, and determine how to reach final reaction:

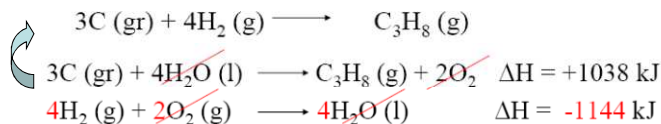
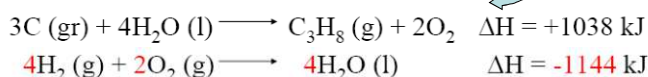


Need to get rid of O₂:

multiply second reaction by 4



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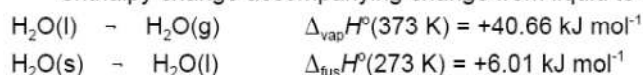
Standard Enthalpy Changes

Numerical values describing ΔU or ΔH of a system when some chemical or physical change occurs depend upon the nature of the reaction, as well as the physical states of reactants and products

It is useful to define a **standard enthalpy change**, ΔH° , which is the change in enthalpy for a process (chemical or physical) where initial and final substances are in **standard states**

standard states: pure form of a substance at specified temperature at pressure of 1 bar, e.g. standard state of liquid water at 298 K is pure liquid water at 298 K and 1 bar

Examples: The standard enthalpy of **vapourization**, $\Delta_{\text{vap}}H^\circ$, is change in enthalpy per mole when pure liquid vapourizes to pure gas at pressure of 1 bar. The standard enthalpy of **fusion**, $\Delta_{\text{fus}}H^\circ$, is enthalpy change accompanying change from liquid to solid



ΔH° can be reported at any temperature, convention is at 298.15 K

Standard enthalpy of formation/reaction

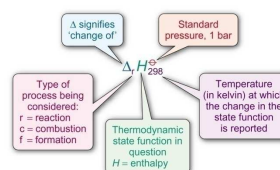
Chemistry³ section 14.3
Kotz section 5.5-5.8.

The standard molar enthalpy of formation is the enthalpy change for the formation of 1 mol of a compound directly from its component elements in their standard states.

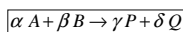
It is not possible to define an absolute measure of enthalpy so a reference State is needed. By convention the enthalpy of formation of an element in its standard state is zero.

The standard state of an element or a compound is defined as the most stable form of the substance in the physical state that exists at a pressure of 1 bar and at a specified temperature (typically 298 K).

The standard enthalpy of formation $\Delta_f H^\circ$ of reactants and products may be used to compute the standard enthalpy change for a chemical reaction $\Delta_r H^\circ$.



Sum of all enthalpy changes of formation of products.



$$\Delta_r H_{298}^\circ = \{\gamma \Delta_f H_{298}^\circ(P) + \delta \Delta_f H_{298}^\circ(Q)\} - \{\alpha \Delta_f H_{298}^\circ(A) + \beta \Delta_f H_{298}^\circ(B)\}$$

$$\Delta_r H_{298}^\circ = \sum_j \nu_j \Delta_f H_{298}^\circ(pr) - \sum_j \nu_j \Delta_f H_{298}^\circ(rx)$$

Stoichiometric coefficient

Sum of all enthalpy changes of formation of reactants.

Standard Molar Enthalpies

Consider the reaction:



Standard enthalpy is calculated from:

$$\Delta_r H^\circ = \sum_{\text{products}} \nu H_m^\circ - \sum_{\text{reactants}} \nu H_m^\circ$$

where ν are stoichiometric coefficients. Thus,

$$\Delta_r H^\circ = [3H_m^\circ(C) + H_m^\circ(D)] - [2H_m^\circ(A) + H_m^\circ(B)]$$

where $H_m^\circ(J)$ is standard molar enthalpy of species J.

Symbolically, we write $0 = 3C + D - 2A - B$, or

$$0 = \sum_J \nu_J J$$

Here J denotes substances and ν_J the stoichiometric numbers,

$$\nu_A = -2 \quad \nu_B = -1 \quad \nu_C = +3 \quad \nu_D = +1$$

Thus, standard reaction enthalpy is: $\Delta_r H^\circ = \sum_J \nu_J H_m^\circ(J)$

Enthalpy of Physical Change

standard enthalpy of transition, $\Delta_{\text{trs}}H^\circ$:

Standard enthalpy change accompanying a phase change

(A) Enthalpy is a *state function*, independent of path between initial and final states: same value of ΔH° occurs regardless of how change occurs!

melting	$\text{H}_2\text{O}(\text{s})$	-	$\text{H}_2\text{O}(\text{l})$	$\Delta_{\text{fus}}H^\circ$
boiling	$\text{H}_2\text{O}(\text{l})$	-	$\text{H}_2\text{O}(\text{g})$	$\Delta_{\text{vap}}H^\circ$
sublimation	$\text{H}_2\text{O}(\text{s})$	-	$\text{H}_2\text{O}(\text{g})$	$\Delta_{\text{sub}}H^\circ = \Delta_{\text{fus}}H^\circ + \Delta_{\text{vap}}H^\circ$

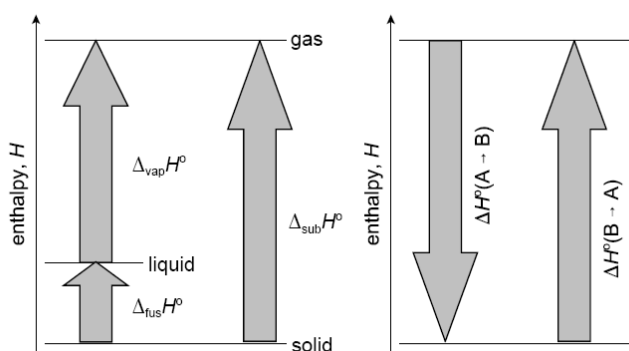
(B) Enthalpy is a *state function*, so ΔH° differs only in sign for forward and reverse processes

$$\Delta H^\circ(\text{A} \rightarrow \text{B}) = -\Delta H^\circ(\text{B} \rightarrow \text{A})$$

Example: At 298 K,

condensing	$\text{H}_2\text{O}(\text{g})$	-	$\text{H}_2\text{O}(\text{l})$	$\Delta_{\text{vap}}H^\circ = -44 \text{ kJ mol}^{-1}$
boiling	$\text{H}_2\text{O}(\text{l})$	-	$\text{H}_2\text{O}(\text{g})$	$\Delta_{\text{vap}}H^\circ = +44 \text{ kJ mol}^{-1}$

Graphical Depiction of Enthalpies of Transition



(A) Same ΔH° , regardless of pathway

(B) Forward & reverse processes, ΔH° differs only in sign

Enthalpies of Fusion and Vapourization

See Table 2.3 Atkins 6th Ed. at back of book for a listing of enthalpies of fusion and vapourization, with freezing and boiling temperatures

Table 2.3 Standard enthalpies of fusion and vaporization at the transition temperature, $\Delta_{\text{tr}}H^\circ$ / (kJ mol⁻¹)

	T_f /K	Fusion	T_b /K	Vaporization	T_f /K	Fusion	T_b /K	Vaporization
Elements								
Ag	1234	11.30	2436	250.6	CO ₂	217.0	8.33	194.6
Ar	83.81	1.188	87.29	6.506	CS ₂	161.2	4.39	319.4
Br ₂	265.9	10.57	332.4	29.45	H ₂ O	273.15	6.008	373.15
Cl ₂	172.1	6.41	239.1	20.41	H ₂ S	187.6	2.377	212.8
F ₂	53.6	0.26	85.0	3.16	H ₂ SO ₄	283.5	2.56	
H ₂	13.96	0.117	20.38	0.916	NH ₃	195.4	5.652	239.7
He	3.5	0.021	4.22	0.084	Organic compounds			
Hg	234.3	2.292	629.7	59.30	CH ₄	90.98	0.941	111.7
I ₂	386.8	15.52	458.4	41.80	CCl ₄	250.3	2.5	350
N ₂	63.15	0.719	77.35	5.586	C ₂ H ₆	89.85	2.86	184.6
Na	371.0	2.601	1156	98.01	C ₆ H ₆	278.61	10.59	353.2
O ₂	54.36	0.444	90.18	6.820	C ₁₀ H ₁₆	-178	13.08	342.1
Xc	161	2.30	165	12.6	C ₁₀ H ₈	354	18.80	490.9
K	336.4	2.35	1031	80.23	CH ₃ OH	175.2	3.16	337.2
Inorganic compounds								
CCl ₄	250.3	2.47	349.9	30.00	C ₂ H ₅ OH	158.7	4.60	352

Data: AP; s denotes sublimation

Enthalpies of Transition †

There are many different types of transitions, each of which has an associated change in enthalpy

Transition	Process	Symbol
Transition	Phase α - Phase β	$\Delta_{\text{trs}}H$
Fusion	s - l	$\Delta_{\text{fus}}H$
Vapourization	l - g	$\Delta_{\text{vap}}H$
Sublimation	s - g	$\Delta_{\text{sub}}H$
Mixing fluids	Pure - mixture	$\Delta_{\text{mix}}H$
Solution	Solute - solution	$\Delta_{\text{sol}}H$
Hydration	X ^z (g) - X ^z (aq)	$\Delta_{\text{hyd}}H$
Atomization	Species(s,l,g) - atoms(g)	$\Delta_{\text{at}}H, \Delta_{\text{diss}}H$
Ionization	X(g) - X ⁺ (g) + e ⁻ (g)	$\Delta_{\text{ion}}H$
Electron gain	X(g) + e ⁻ (g) - X ⁻ (g)	$\Delta_{\text{eg}}H$
Reaction	Reactants - products	Δ_rH
Combustion	Cmpd(s,l,g) + O ₂ (g) - CO ₂ (g) + H ₂ O(l,g)	Δ_cH
Formation	Elements - compound	Δ_fH
Activation	Reactants - activated complex	$\Delta^\ddagger H$

Variation of enthalpy of a substance with temperature

The enthalpy of a substance increases with temperature. Now enthalpy change is the heat transferred at constant pressure. Let q_p is the energy used to heat a substance in an open container from an initial temperature T_1 to a final temperature T_2 . Hence the enthalpy change is

$$\Delta H(T_1 \rightarrow T_2) = q_p$$

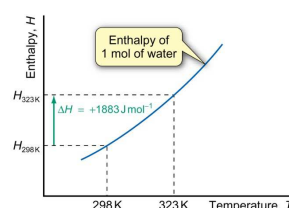
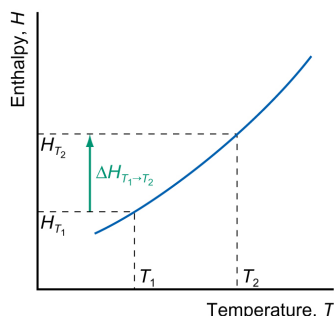
Now q_p is given by

$$q_p = nC_{p,m}\Delta T = nC_{p,m}(T_2 - T_1)$$

Hence

$$\begin{aligned} \Delta H(T_1 \rightarrow T_2) &= H(T_2) - H(T_1) \\ &= C_{p,m}\Delta T = C_{p,m}(T_2 - T_1) \end{aligned}$$

Note that $H(T)$ variation is a curve rather than a straight line since $C_{p,m}$ also varies with temperature.

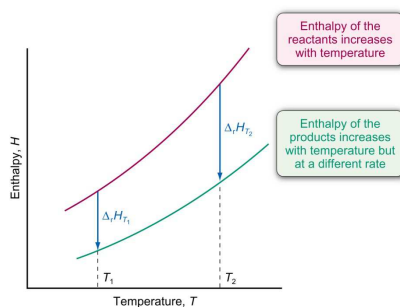


Variation of enthalpy of a reaction with temperature: Kirchoff equation.

If the enthalpy change for a reaction $\Delta_r H(T_1)$ is known at the temp. T_1 , then the value $\Delta_r H(T_2)$ at another temp. T_2 can be determined using the Kirchoff equation.

$$\Delta_r H^0(T_2) = \Delta_r H^0(T_1) + \Delta C_{p,m} \Delta T$$

Note that $\Delta C_{p,m}$ denotes the difference between the molar heat capacity of the products and the molar heat capacity of the reactants.



Derivation provided in Chemistry³ Box 14.5 p.683. See worked example p.684.

$$\Delta C_{p,m} = \sum \nu_j C_{p,m}(pr) - \sum \nu_j C_{p,m}(rx)$$